

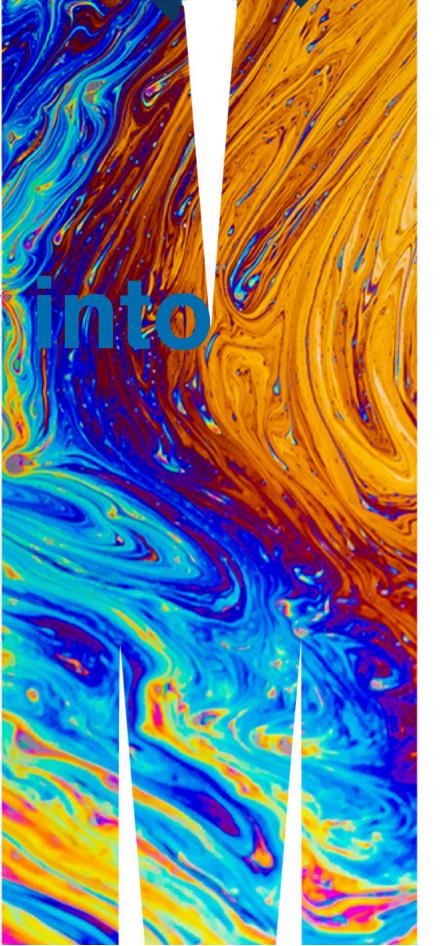
ETC5521: Diving Deeply Data Exploration

Week 2: Learning from history

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Department of Econometrics and Business Statistics

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Birth of EDA

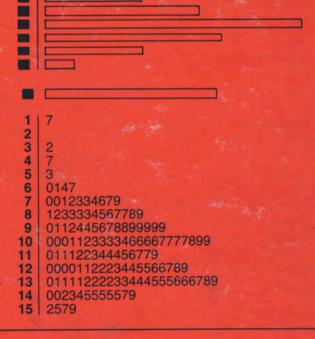
The field of exploratory data analysis came of age when this book appeared in 1977.

Tukey held that too much emphasis in statistics was placed on statistical hypothesis testing (confirmatory data analysis); more emphasis needed to be placed on using data to suggest hypotheses to test.

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Tukey

ORATORY DATA



John W. Tukey



- Born in 1915, in New Bedford, Massachusetts.
- Mum was a private tutor who homeschooled John. Dad was a Latin teacher. BA and MSc in Chemistry, and PhD in
- **Mathematics**
- Awarded the National Medal of Science in 1973, by President Nixon
- By some reports, his home-schooling was unorthodox and contributed to his thinking and working differently.

Image source: wikimedia.org

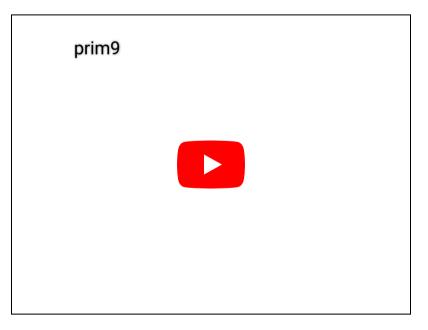
Taking a glimpse back in time

is possible with the American Statistical Association video lending library.

We're going to watch John Tukey talking about exploring high-dimensional data with an amazing new computer in 1973, four years before the EDA book.

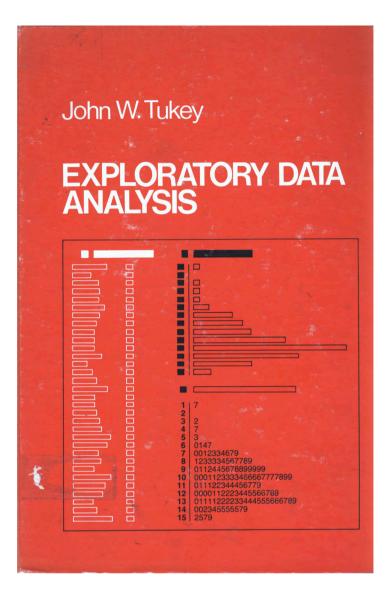
Look out for these things:

Tukey's expertise is described as for trial and error learning and the computing equipment.



First 4.25 minutes

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Everything in this book can be dere with pencil and paper 11

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Setting the frame of mind

Excerpt from the introduction

This book is based on an important principle.

It is important to understand what you CAN DO before you learn to measure how WELL you seem to have DONE it.

Learning first what you can do will help you to work more easily and effectively.

This book is about exploratory data analysis, about looking at data to see what it seems to say. It concentrates on simple arithmetic and easy-to-draw pictures. It regards whatever appearances we have recognized as partial descriptions, and tries to look beneath them for new insights. Its concern is with appearance, not with confirmation.

Examples, NOT case histories

Outline

- 1. Scratching down numbers
- 2. Schematic summary
- 3. Easy re-expression
- 4. Effective comparison
- 5. Plots of relationship
- 6. Straightening out plots (using three points)
- 7. Smoothing sequences
- 8. Parallel and wandering schematic plots
- 9. Delineations of batches of points
- 10. Using two-way analyses

- 11. Making two-way analyses
- 12. Advanced fits
- 13. Three way fits
- 14. Looking in two or more ways at batched of points
- 15. Counted fractions
- 16. Better smoothing
- 17. Counts in bin after bin
- 18. Product-ratio plots
- 19. Shapes of distributions
- 20. Mathematical distributions

Looking at numbers with Tukey



Scratching down numbers

Prices of Chevrolet in the local used car newspaper ads of 1968.

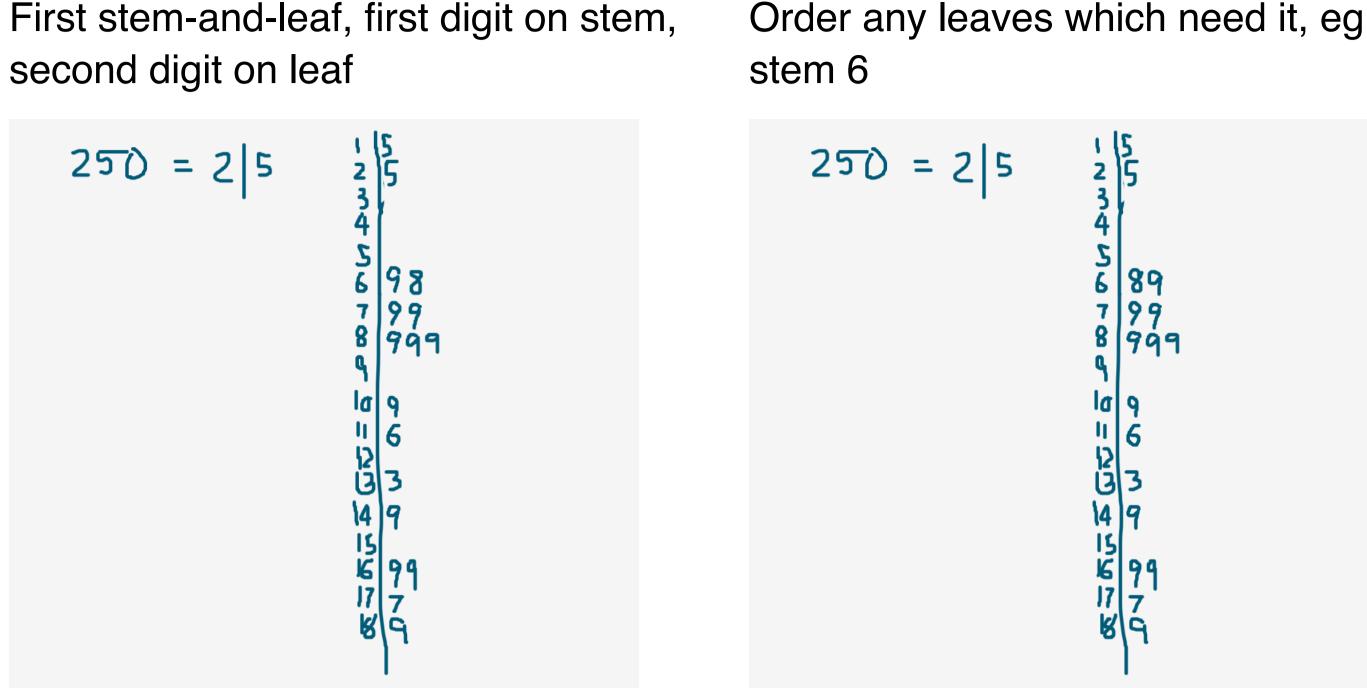
1	options(width=20)
2	chevrolets <- tibble(
3	prices = c(250, 150, 795, 895, 695,
4	1699, 1499, 1099, 1693, 1166,
5	688, 1333, 895, 1775, 895,
6	1895, 795))
7	#chevrolets\$prices

Stem-and-leaf plot: statistics texts

	kport		
250,	150,	795 ,	895,
1699,	1499	, 109	99, 10
1166,	688,	1333	3, 895
1775,	895,	1895	5, 795

Stem-and-leaf plot: still seen in introductory

- 695,
- 693,
- 5,
- 5



A benefit is that the numbers can be read off the plot, but the focus is still on the pattern. Also quantiles like the median, can be computed easily.



Shrink the stem

55 1 3 5.89 99999 7. ٩. 11.6 13-39 اكا 17. 9

Shrink the stem more

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i 8999 63 79

And, in R ...

1 ch	nevrolets <mark>\$prices</mark>
<pre>[1] 250 150 [4] 895 695 [7] 1499 1099 [10] 1166 688 [13] 895 1775 [16] 1895 795</pre>	1693 1333 895
1 st	tem(chevrolets\$prices)
The decimal p 0 23 0 7788999 1 123	point is 3 digit(s) to the right of the

Remember the tips data

[1] 1.01 1.66 3.50 3.31 3.61 4.71 2.00 3.12 1.96 3.23 1.71 5.00 1.57 3.00 3.02 [16] 3.92 1.67 3.71 3.50 3.35 4.08 2.75 2.23 7.58 3.18 2.34 2.00 2.00 4.30 3.00 [31] 1.45 2.50 3.00 2.45 3.27 3.60 2.00 3.07 2.31 5.00 2.24 2.54 3.06 1.32 5.60 [46] 3.00 5.00 6.00 2.05 3.00

1 stem(tips\$tip, scale=0.5, width=120)

The decimal point is at the

- 1 | 00000123333444555555555555566666667777788889

- 4 | 000000000001112233335777
- 5 | 0000000001122226799
- 6 | 05577

0

7 | 6

8

- 9
- 10 | 0

Refining the size

			(#)
3.	8	Tate	(1)
4*	0121243121300214202	2	(19)
4 ·	597886556569		(12)
5*	142010		(6)
5·	977899958797		(12)
6*	412441		(6)
6·	898598		(6)
7*	320341203		(9)
7 ·	86657		(5)
8*	303		(3)
8 ·	8	Hinds	(1)
9*	24	Bolivar, Yazoo	(2)

What is the number in parentheses? And why might this be useful?

Two digits per stem				
A) FIVE-LINE VERSION				
		(#)		
1*	1	(1)		
t	2333 445555	(4)		
f	445555	(6)		
S	66677	(5)		
•	88	(2)		
2*	0000011	(7)		
t	23	(2)		
f	445	(3)		
S	6	(1)		
•	9	(1)		
3*	1	(1)		
t	3	(1)		
t f s	;			
S				
•		(34√)		

	1 stem(tips <mark>\$</mark> tip
The	decimal point is 1 o
10	0000107
12	55526
14	4457800000000678
16	1346781356
18	032678
20	000000000000000000000000000000000000000
22	0033440114
24	570000000002456
26	01412455
28	382
30	000000000000000000000000000000000000000
32	133557159
24	
Why	no number in

		1	median(tips <mark>\$</mark> ti
[1]	2.9		

, scale=2)

digit(s) to the left of the |

0000000000000011233598

000000267891245688

parentheses?

ip)

Summary

- Stem-and-leaf plots are similar information to the histogram.
- Generally it is possible to also read off the numbers, and to then easily calculate median or Q1 or Q3.
- It's great for small data sets, when you only have pencil and paper.
- Alternatives are a histogram, (jittered) dotplot, density plot, box plot, violin plot, letter value plot.

a different style of number scratching

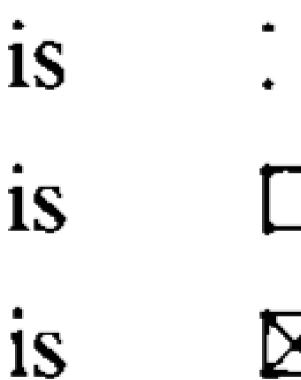
for categorical variables

We know about

Is this easier?

11 111 1111 THA but its too easy to 8 or 10 make a mistake

or harder



Count this data using the squares approach.

"F" "M" "M" "M" "F" "M" [1] "M" "M" "M" "M" "F" [7] "M" "M" "F" "M" "F" "M" [13] "F" "M" "M" "F" "F" "M" [19] "M" "M" "M" "M" "M" "F" [25] "M" "M" "F" "F" "M" "M" [31] "M" "F" "M" "M" "M" "M" [37] "M" "M" "M" "M" "M" "M" [43] "M" "M" "M" "F" "F" "M" [49] "M" "M" "M" "F" "M" "M" [55] "M" "M" "M" "M" "M" [61] "F" "F" "M" "M" "M" "F" [67]

Export



What does it mean to "feel what the data are like?"

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exhibit **10** of chapter 1: state heights

The heights of the highest points in each state

_			(#)
0*	43588	Del, Fla, La, Miss, Rl	(5)
1	237886		(6)
2	484030		(6)
3	45526		(5)
4*	80149		(5)
5	34307		(5)
6	376		(3)
7	2	S. Dak	(1)
8*	8	Texas	(1)
9	0		(1)
10	0	0	(1)
11	2	Oregon	(1)
12*	768		(3)
13	81258		(5)
14	544	Calif, Colo, Wash	(3)
15			
16*			
17			
18			
19			

Alaska

20* 3

It's not really surprising, but we can imagine this peaks, and the rest of the states lump together.

(1) (50, √) ETC5521 Lecture 2 | ddde.numbat.space

This is a stem and leaf of the height of the highest peak in each of the 50 US states.

- The states roughly fall into three groups.
- grouping. Alaska is in a group of its own, with a much higher high peak. Then the Rocky Mountain states, California, Washington and Hawaii also have high

Exploratory data analysis is detective work – in the purest sense – finding and revealing the clues.

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More summaries of numerical values

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Hinges and 5-number summaries

```
[1] -3.2 -1.7 -0.4 0.1
[5] 0.3 1.2 1.5 1.8
[9] 2.4 3.0 4.3 6.4
[13] 9.8
```

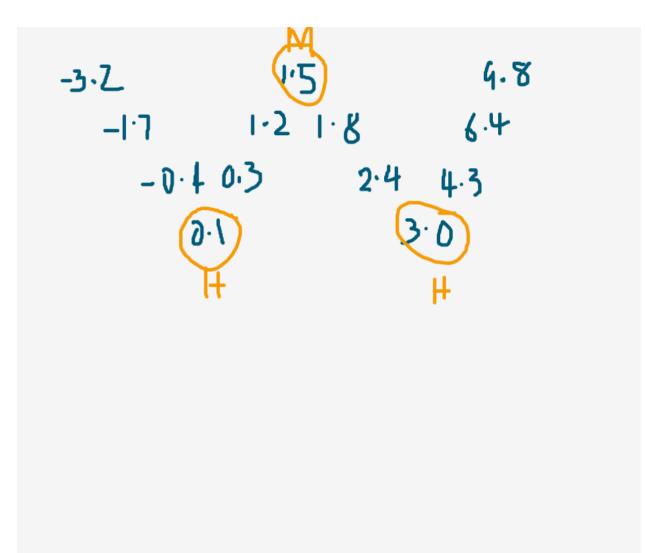
You know the median is the middle number. What's a hinge?

There are 13 data values here, provided already sorted. We are going to write them into a Tukey named down-up-down-up pattern, evenly.

Median will be 7th, hinge will be 4th from each end.

	Export
-	

Hinges and 5-number summary



Hinges illustrated

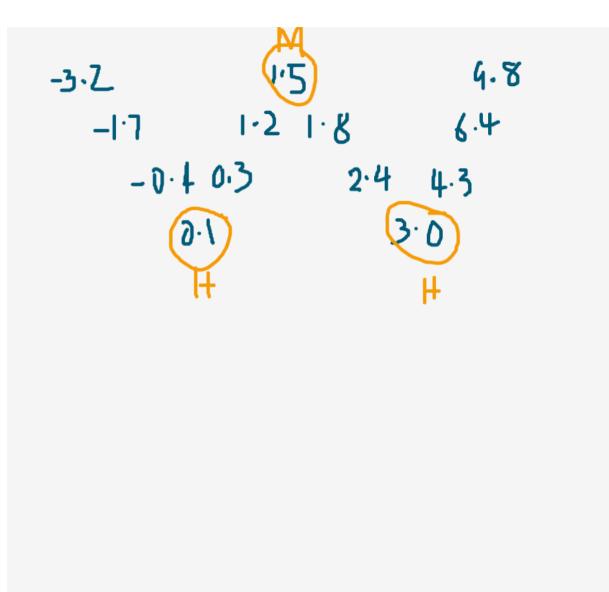
A)	The 17 Al	JTO PRICES	6 of EX
(1) 150		(N 89	•
25	0	895	1099
	688	895	1
	695	795	
	79	5	
	(H)	

[17 prices, 1HMH1: 150, 795, 895, 1499, 1895 dollars]

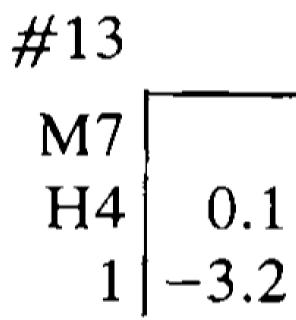
Hinges are almost always the same as Q1 and Q3

XHIBIT 1—in folded form (1) 1895 9 1775 1166 1699 1333 1693 1499 (H)

box-and-whisker display



Starting with a 5-number summary



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1.5 3.0 9.8

box-and-whisker display

Starting with a 5-number summary



Identified end values



Why are some individual points singled Rules for this out?

Rules for this one may be clearer?

Isn't this imposing a belief?

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There is no excuse for failing to plot and look

Another Tukey wisdom drop

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Fences and outside values

- H-spread: difference between the hinges (we would call this Inter-Quartile Range)
- step: 1.5 times H-spread
- inner fences: 1 step outside the hinges
- outer fences: 2 steps outside the hinges
- the value at each end closest to, but still inside the inner fence are "adjacent"
- values between an inner fence and its neighbouring outer fence are "outside"
- values beyond outer fences are "far out"
- these rules produce a SCHEMATIC PLOT





New statistics: trimeans

The number that comes closest to

lower hinge $+ 2 \times \text{median} + \text{upper hinge}$

4

is the trimean.

Think about trimmed means, where we might drop the highest and lowest 5% of observations.

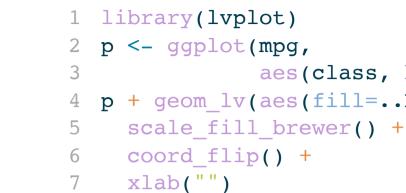
Letter value plots

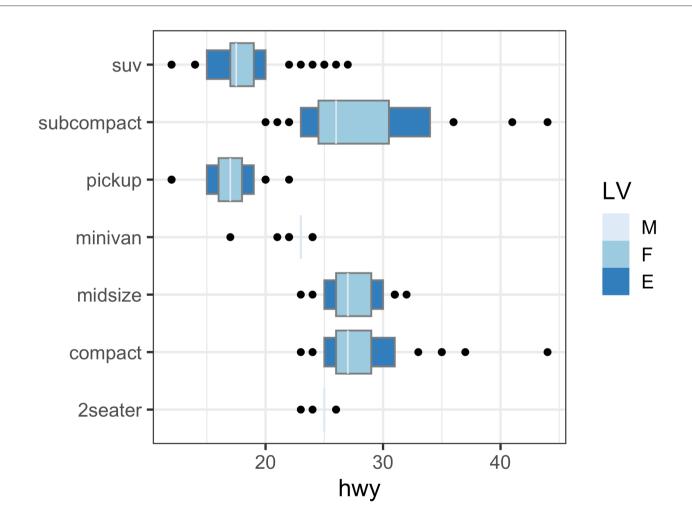
Why break the data into quarters? Why not eighths, sixteenths? k-number summaries? What does a 7-number summary look like?

(Seven-number summary)	
(Devenimentaline adminiary)	

50	popu	lations	
M25h H13	24	6	
H13	89	432	343 (H-spread)
E7	63	782	719 (E-spread)
1	23	1678	343 (H-spread) 719 (E-spread) 1655 (range)

How would you make an 11-number summary?





```
aes(class, hwy))
p + geom_lv(aes(fill=..LV..)) +
```

Box plots are ubiquitous in use today.

- Mostly used to compare distributions, multiple subsets of the data.

• Puts the emphasis on the middle 50% of observations, although variations can put emphasis on other aspects.

Easy re-expression



Logs, square roots, reciprocals

What you need to know about logs?

- how to find good enough logs fast and easily
- that equal differences in logs correspond to equal ratios of raw values.

(This means that wherever you find people using products or **ratios**— even in such things as price indexes-using logs-thus converting producers to sums and ratios to differences—is likely to help.)

The most common transformations are logs, sqrt root, reciprocals, reciprocals of square roots

What happened to ZERO?

solved by the logarithm.

- -1, -1/2, +1/2, +1
- It turns out that the role of a zero power, is for the purposes of re-expression, neatly

Re-express to symmetrize the distribution

Deaths for 59 selected causes, 1964 (total 1,798,051, less "all other diseases 54,000")

A) SMALL COUNTS

Raw	Log	Cause
17	1.23	Polio
42	1.62	Diphtheria
93	1.97	Whooping cough (WC below)
95	1.98	Scarlet fever and strep throat (SFST below)

B) RAW VALUES--in 100's C) LOGS--in 0.1's

0*	7,3,8,4,2	•]	
	7,8,3,1	S	7	Polio
2	6,5	s f		
3	5,8	t	3	Diph
4	9,4,6,4	-0*	00	WC,SFST
5*	9,4	0*		
6	5	t	3	Abortion
7	6	t f	4	Dysentery
8	2	S	6	Measles
9*	9,9,8	•	89	
		1*	01	
1**	35,35,67,59,22,11,10	t	22	
2	62,77,57,34,32,03,52,53,06	f	4455	
3	28,23,72,07	S	666677	
4	92,00,69	•	8899	
5**	32,74,78,69	2*	00000011	
		t	23333	
0***	932,	f	44444555	
1***	982,	S	6667777	
2		•	9 †	
3		3*		
4***	454,	t	3†	
		f		
		S	7 †	
		•		

Power ladder

G fix RIGHT-skewed values

-2, -1, -1/2, 0 (log), 1/3, 1/2, **1**, 2, 3, 4

fix LEFT-skewed values

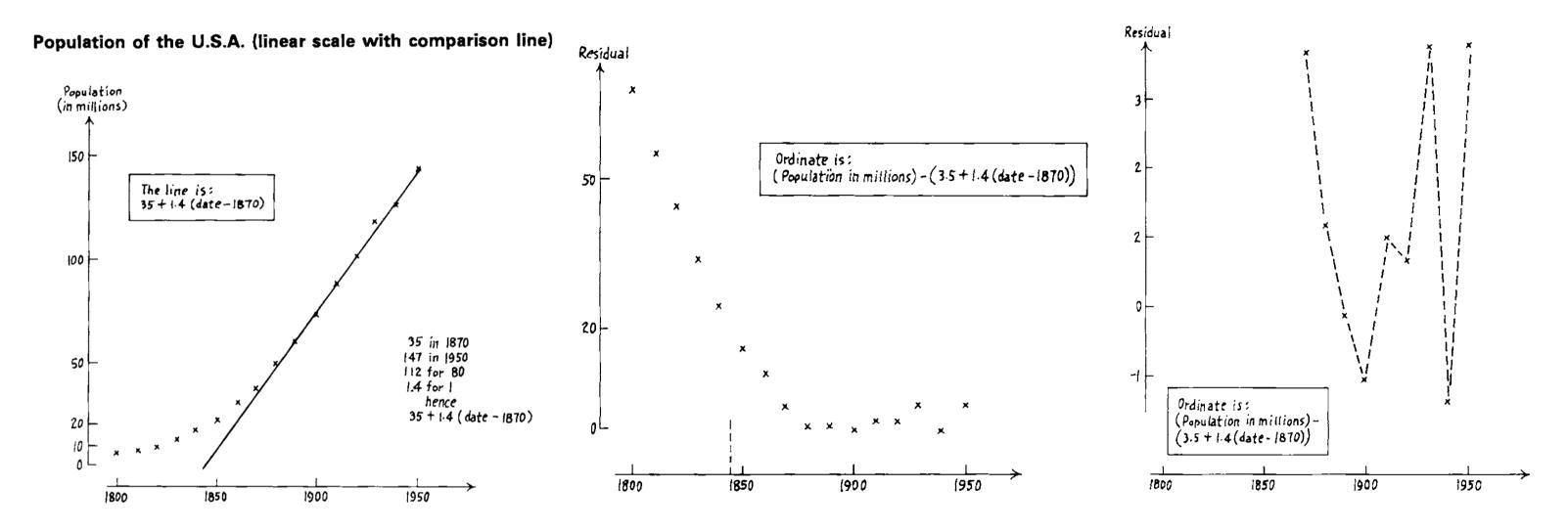
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We now regard re-expression as a tool, something to let us do a better job of grasping. The grasping is done with the eye and the better job is through a more symmetric appearance.

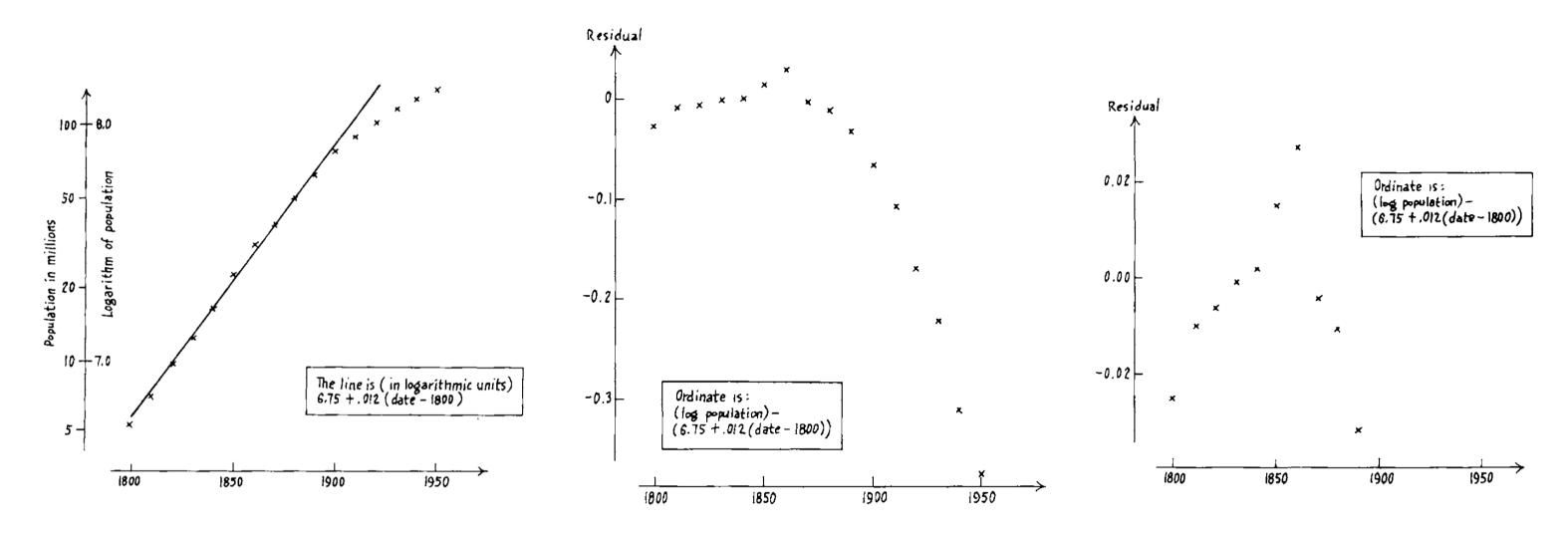
Another Tukey wisdom drop

Linearising bivariate relationships



Surprising observation: The small fluctuations in later years. What might be possible reasons?

Linearising bivariate relationships



See some fluctuations in the early years, too. Note that the log transformation couldn't linearise.

Whatever the data, we can try to gain by straightening or by flattening. When we succeed in doing one or both, we almost always see more clearly what is going on.

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Rules and advice

- 1. Graphics are friendly.
- 2. Arithmetic often exists to make graphs possible.
- 3. Graphs force us to notice the unexpected; nothing could be more important.
- 4. Different graphs show us quite different aspects of the same data.
- 5. There is no more reason to expect one graph to "tell all" than to expect one number to do the same.
- 6. "Plotting y against x" involves significant choices—how we express one or both variables can be crucial.

- reasonable.
- another.
- concealment by crowding.

7. The first step in penetrating plotting is to straighten out the dependence or point scatter as much as

8. Plotting y^2 , \sqrt{y} , $\log(y)$, -1/y or the like instead of y is one plausible step to take in search of straightness. 9. Plotting x^2 , \sqrt{x} , $\log(x)$, -1/x or the like instead of x is

10. Once the plot is straightened, we can usually gain much by flattening it, usually by plotting residuals.

11. When plotting scatters, we may need to be careful about how we express x and y in order to avoid

The book is a digest of 🛱 tricks and treats 🛱 of massaging numbers and drafting displays.

Many of the tools have made it into today's analyses in various ways. Many have not. ord "software" Notice the word developments too: froots, fences. Tukey brought yo The temperament of the book is an inspiration for the mind-set for this unit. The re is such delight in working with numbers!

"We love data!"

Take-aways

- Tukey's approach was a reaction to many years of formalising data analysis using statistical hypothesis testing.
- Methodology development in statistical testing was a reaction to the ad-hoc nature of data analysis.
- Complex machine learning models like neural networks are in reaction to the inability of statistical models to capture highly non-linear relationships, and depend heavily on the data provided.
- Exploring data today is in reaction to the need to explain complex models, to support organisations against legal challenges to decisions made from the model
- It is much easier to accomplish computers.
- "Exploratory data analysis" as commonly used today term is unfortunately synonymous with "descriptive statistics", but it is truly much more. Understanding its history from Tukey's advocation helps you see it is the tooling to discover what you don't know.

Resources

- wikipedia
- John W. Tukey (1977) Exploratory data analysis
- Data coding using tidyverse suite of R packages
- Sketching canvases made using fabricerin